

1. Solve each equation.

$$a) 16^{n-7} + 5 = 24$$

$$16^{n-7} = 19$$

$$\log_{16} 19 = n-7$$

$$\frac{\log 19}{\log 16} = n-7$$

$$1.06 = n-7$$

$$\boxed{8.06 = n}$$

$$c) \log x + \log 8 = 2$$

$$\log_{\cancel{8}}^x \log 8x = 2$$

$$10^2 = 8x$$

$$100 = 8x$$

$$\boxed{12.5 = x}$$

$$b) 3.7e^{2-2n} - 9 = -4$$

$$3.7e^{2-2n} = 5$$

$$\cancel{3.7} e^{2-2n} = 1.47$$

$$\ln 1.47 = 2-2n$$

$$.39 = 2-2n$$

$$-1.61 = -2n$$

$$\boxed{.805 = n}$$

$$d) \ln(-3x-1) - \ln 7 = 2$$

$$\ln \frac{-3x-1}{7} = 2$$

$$e^2 = \frac{-3x-1}{7}$$

$$7.39 = \frac{-3x-1}{7}$$

$$51.72 = -3x-1$$

$$52.72 = -3x$$

$$\boxed{-17.57 = x}$$

2. Differentiate each function with respect to x .

$$a) y = \ln(\cos x)$$

$$= \frac{1}{\cos x} \cdot -\sin x$$

$$= \frac{-\sin x}{\cos x}$$

$$\boxed{\frac{dy}{dx} = -\tan x}$$

$$b) y = \ln\left(\frac{2x^2}{x^2+3}\right)$$

$$= \ln 2x^2 - \ln x^2 + 3$$

$$= \frac{1}{2x^2} \cdot 4x - \frac{1}{x^2+3} \cdot 2x$$

$$\boxed{\frac{dy}{dx} = \frac{2}{x} - \frac{2x}{x^2+3}}$$

$$c). y = \log_3 8x^3$$

$$= \frac{1}{8x^3 \ln 3} \cdot 24x^2$$

$$\frac{dy}{dx} = \frac{24x^2}{8x^3 \ln 3} = \boxed{\frac{3}{x \ln 3}}$$

$$e). y = e^{2x^3}$$

$$\frac{dy}{dx} = e^{2x^3} \cdot 6x^2$$

$$d). y = 4(x^5+1)^3$$

$$= 4(x^5+1)^3 \cdot 3(x^5+1)^2 \cdot 5x^4$$

$$\frac{dy}{dx} = \boxed{4(x^5+1)^3 \cdot 15x^4(x^5+1)^2}$$

$$f). y = \ln(4x^2+3)^4$$

$$= \frac{1}{(4x^2+3)^4} \cdot 4(4x^2+3)^3 \cdot 8x$$

$$\frac{dy}{dx} = \frac{32x(4x^2+3)^3}{(4x^2+3)^4} = \boxed{\frac{32x}{4x^2+3}}$$

③ Use logarithmic differentiation to differentiate each function with respect to x.

$$a). y = (2x^3+1)^2 (x+3)^4$$

$$\ln y = \ln(2x^3+1)^2 + \ln(x+3)^4$$

$$\ln y = 2 \ln(2x^3+1) + 4 \ln(x+3)$$

$$\frac{1}{y} \cdot \frac{dy}{dx} = 2 \cdot \frac{1}{2x^3+1} \cdot 6x^2 + 4 \cdot \frac{1}{x+3} \cdot 1$$

$$\frac{dy}{dx} = \left(\frac{12x^2}{2x^3+1} + \frac{4}{x+3} \right) (2x^3+1)^2 (x+3)^4$$

$$b). y = \frac{(x^2+4)^4}{(3x^2-5)^2}$$

$$\ln y = \ln(x^2+4)^4 - \ln(3x^2-5)^2$$

~~$$\frac{1}{y} \cdot \frac{dy}{dx} = \frac{4}{x^2+4} - \frac{2}{3x^2-5} \cdot 6x$$~~

$$\frac{1}{y} \cdot \frac{dy}{dx} = 4 \ln(x^2+4) - 2 \ln(3x^2-5)$$

$$\frac{1}{y} \cdot \frac{dy}{dx} = 4 \cdot \frac{1}{x^2+4} \cdot 2x - 2 \cdot \frac{1}{3x^2-5} \cdot 6x$$

$$= \left(\frac{8x}{x^2+4} - \frac{12x}{3x^2-5} \right) \left(\frac{(x^2+4)^4}{(3x^2-5)^2} \right)$$

④ Use l'Hopital's Rule, if applicable, to find the limit.

$$a). \lim_{x \rightarrow \infty} \frac{8x}{e^{3x}} = \frac{\infty}{\infty}$$

$$\frac{8}{3e^{3x}} = \lim_{x \rightarrow \infty} \frac{8}{3e^{3x}} = \frac{8}{\infty} = 0$$